Appearance and Structure Aware Robust Deep Visual Graph Matching: Attack, Defense and Beyond

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Abstract

Despite the recent breakthrough of high accuracy deep graph matching (GM) over visual images, the robustness of deep GM models is rarely studied which yet has been revealed an important issue in modern deep nets, ranging from image recognition to graph learning tasks. We first show that an adversarial attack on keypoint localities and the hidden graphs can cause significant accuracy drop to deep GM models. Accordingly, we propose our defense strategy, namely Appearance and Structure Aware Robust Graph Matching (ASAR-GM). Specifically, orthogonal to de facto adversarial training (AT), we devise the Appearance Aware Regularizer (AAR) on those appearance-similar keypoints between graphs that are likely to confuse. Experimental results show that our ASAR-GM achieves better robustness compared to AT. Moreover, our locality attack can serve as a data augmentation technique, which boosts the state-of-the-art GM models even on the clean test dataset.

1. Introduction

Graph matching (GM), as one of the most important research topics in the graph domain with wide applications in vision and pattern recognition, aims to find node-to-node correspondence among graphs. The matching of visual graphs has been intensively studied over the decades, such as image keypoint matching [42], scene graph discovery [6], and vision-text retrieval [46], especially since the recent advances in combining deep neural networks and (visual) GM [51]. Despite the success of deep GM, deep neural networks (DNN)s are found vulnerable to small input perturbations which are imperceptible to humans [3, 38]. For example, in image classification, carefully designed small perturbations on image pixels can fool neural classifiers [18], and in graph domain, attackers perturb graph structures and its attributes to cause failures of graph learning tasks such as node class-

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linear interpolation and directly determines the graph structure derived by Delaunay triangulation. However, the location of keypoints suffers from its inherent instability due to the randomness of human labeling or keypoint detectors, which means small yet malicious noise could be easily added without being detected. Therefore, we propose to perturb keypoint locality as an effective adversarial attack.

Towards defending against adversarial attacks, adversarial training (AT) [30] has become a widely-recognized principle defense mechanism by training models on adversarial examples while it suffers from lowering accuracy on clean test examples. Moreover, for graph learning, there are efforts in improving robustness against adversarial attacks in node classification [47, 54, 58], graph classification [25], community detection [21], etc. However, those defense mechanisms only focus on single graph learning tasks while GM learns to analyze intersections among graphs such that these methods cannot be directly applied to GM. In this paper, based on our analysis of the vulnerability of GM, we explore a new way of defending against adversarial attacks.

Our defense mechanism derives from two insights. First, we show that that adversarial attacks tend to confuse keypoints with similar appearance and those appearance-similar keypoints usually occur in three cases: (1) shape similarity, e.g. the two ears of a cat; (2) texture similarity, e.g. the wither and tail of a cat; (3) structural symmetry, e.g. the four roof corners of a car. Such appearance-similarity depends on some prior in the dataset. For two graphs, if we can select these appearance-similar keypoints between them and explicitly enlarge their disparity in the probabilistic space of model outputs, the model robustness could get enhanced. Moreover, since our regularization strategy works in output space, which is orthogonal to AT that generates worst-case example in input space, we can further improve model robustness by combining them together.

To this end, we take the initiative on studying the robustness of visual GM. On the attacker’s side, we propose an effective keypoint locality attack and combine it with pixel attack to devise an even stronger attack. For defense, we analyze the attack pattern and discover that those appearance-similar keypoints can be inferred from the result of our adversarial attack. Then we design a regularization term, namely Appearance Aware Regularizer (AAR), to regularize the discrepancy of features of keypoints which share similar appearance in the low-dimensional embedding space. Finally, we propose our defense strategy, namely Appearance and Structure Aware Robust Graph Matching (ASAR-GM) on the basis of AT. The highlights are:

1) We analyze the vulnerability of deep (visual) graph matching (GM) under adversarial attacks and design an effective locality attack, which perturbs the keypoint locations and hidden graph structure together. Moreover, stronger adversarial data is generated by combining our locality attack and pixel attack together. Our work differs from two recent GM attack/defense works as they only focus on adding/deleting the edges without manipulating on visual images as also considered in our method (see Table 1).

2) We propose our defense strategy, namely Appearance and Structure Aware Robust Graph Matching (ASAR-GM) to enhance robustness. Specifically, we show that adversarial attacks tend to utilize appearance-similar keypoints among graphs to fool the matching of the model. As such, we design a regularization term: Appearance Aware Regularizer (AAR), to enlarge the disparity among appearance-similar keypoints in graph. Our AAR can be naturally integrated into the framework of AT, which brings better clean accuracy and robustness.

3) Experiments on real-world benchmarks validate the effectiveness of our attack on various deep GM baselines [34, 42, 48] including the state-of-the-art NGMv2 [44]. Our attack also shows strong transferability in the black-box attack setting. For defense, ASAR-GM achieves better clean accuracy and robustness over defense baselines.

4) Last but importantly, while adversarial examples are often viewed a threat to DNN, our locality attack serves as a data augmentation to improve generalization ability of deep GM because perturbations on locality induce various graph structures for training, making our model a new GM SOTA.

### 2. Related Work

**Deep Graph Matching.** The pioneer work [31] considers graph alignment by embedding on individual graphs. With the remarkable performance of deep neural networks (DNNs) in vision, deep learning has been applied for GM on images since the proposal of the seminal work [51], which utilizes a convolutional neural network (CNN) to extract node features and builds an end-to-end model with spectral matching. Since then, deep (visual) GM has become a trending topic: [17, 23, 42, 43, 55, 57] introduce graph
neural networks (GNN)s [35] to improve GM by encoding graph structural information; [48] proposes an edge embedding module and Hungarian-based attention mechanism; the work [34] proposes an end-to-end deep GM architecture combining unmodified combinatorial solvers with deep learning together; NGMv2 [44], as our main defense baseline model in Paper, deals with the general Lawler’s QAP form [29], which solves GM via applying vertex classification on the association graph. By adopting more advanced feature extractors e.g. [15], NGMv2 achieves the state-of-the-art performance for deep GM.

Adversarial Attack & Defense on GM. [56] focuses on dealing with the raw graph data without vision information. It generates adversarial examples by maximizing a node density estimation function built by kernel density estimation (KDE) during a meta-learning-based PGD attack. They craft adversarial data by inserting/deleting edges. However, such an attack is NOT feasible for visual GM, because firstly, the construction of (visual) graphs is determined by certain domain knowledge, e.g. Delaunay triangulation; secondly, the perturbed edges are no longer “imperceptible” and could be detected and recovered easily. [33] enhances the robustness of traditional GM by penalizing the dense region of nodes against the node density attack [56], and detecting the adversarial examples from the inputs, which are different from our proactive defense, i.e., increasing robustness of the victim models against adversarial examples. This paper also differs from papers studying the robustness of object tracking [22,28], where only the visual features are considered. The recent work [50] enhances the robustness of visual GM against “natural” noise in images e.g. deformations, rotations, and outliers. But it does not consider to defend against the designed adversarial attacks.

3. Preliminaries

3.1. Problem Definition

We mainly focus on the visual GM task: given an image pair $c=(c^1, c^2)$, each of them is annotated with $n$ keypoints, and their annotated keypoint locality set $z=(z^1, z^2)$, where $z^1, z^2 \in \mathbb{R}^{n \times 2}$. Moreover, we treat the hidden keypoint graphs $G=(G^1, G^2)$ as the general attribute graph, i.e., $G^1 = \{V^1, E^1, G^1, H^1\}$ and $G^2 = \{V^2, E^2, G^2, H^2\}$. Here $V$ is the node set, $E$ is the edge set and $|V^1|=n, |E^1|=m_1, |V^2|=n, |E^2|=m_2$. The connectivity of two graphs are represented by $G^1, H^1 \in \{0,1\}^{n \times m_1}$ and $G^2, H^2 \in \{0,1\}^{n \times m_2}$, where $G_{i,k} = H_{i,k} = 1$ means edge $k$ links node $i$ to node $j$ and $A^1 = G^1 H^1^T, A^2 = G^2 H^2^T$ are the adjacency matrices of two graphs.

**Graph matching.** It can be written as quadratic assignment programming (QAP) [29], where $X \in \mathbb{R}^{n \times n}$ is a permutation matrix for node-to-node correspondence$^1$, and vec($X$) is its column-vectorized version:

$$\max J(X) = \text{vec}(X)^T K \text{vec}(X)$$

s.t. $X \in \{0, 1\}^{n \times n}, X1_n = 1_n, X^T 1_n = 1_n$  \hspace{1cm} (1)

where $K \in \mathbb{R}^{n \times n}$ is the affinity matrix whose diagonal and off-diagonal elements store the node-to-node and edge-to-edge affinities. The goal of GM is to maximize the objective $J(X)$ with the assumption that perfect matching corresponds to the highest affinity score.

**Deep graph matching.** To enable end-to-end learning, Lawler’s QAP in Eq. 1 is relaxed via (partial) doubly-stochastic relaxation for $S$ whose rows/columns sum to 1:

$$\max J(S) = \text{vec}(S)^T K \text{vec}(S)$$

s.t. $S \in [0,1]^{n \times n}, S1_n = 1_n, S^T 1_n = 1_n$  \hspace{1cm} (2)

Deep GM methods recently proposed deal with images with keypoints as inputs and solve such QAP problem in Eq. 2 in an end-to-end manner [34,42–44,48,51,55]. As Fig. 2 shows, these methods usually consist of three components: keypoint feature extractor, affinity learning, and final correspondence solver. Let $f$ denote the CNN layers taking image pairs $(c^1, c^2)$ for node (and edge) feature extraction, $g$ denote the affinity learning layer for generating the affinity matrix $K$, and the correspondence solver $h$ for the final permutation. In this paper, we focus on the vulnerability of the current state-of-the-art model NGMv2 [44], where the matching problem is translated into a vertex classification task and binary cross-entropy (BCE) loss is utilized.

3.2. Adversarial Attack

For clarity, here we only consider adversarial attacks on image pixel. We denote the end-to-end deep GM pipeline as $M : (c^1, c^2) \in \mathbb{R}^D \rightarrow X \in \{0, 1\}^{n \times n}$. Adversarial attack usually aims to find the worst-case example within a ball around the clean sample, $B_\epsilon(c) = \{ c' : d_p(c, c') \leq \epsilon \}$, and $d_p(c, c') = ||c' - c||_p$ is the similarity metric, where $\ell$-\infty norm is chosen in our experiment.

**White-box Attack.** In the white-box setting, the attacker has the access to full information of models. Following Fast Gradient Sign Method (FGSM) [18] which adds perturbations along the direction of gradient descent, a popular and effective iterative gradient-based method, Projected Gradient Descent (PGD) attack [30], is proposed:

$$c'_{k+1} = \Pi_{B_\epsilon(c)}(c'_k + \alpha \text{sign}(\nabla_{c'_k} L(M(c'_k), y; \theta)))$$

where $\Pi_{B_\epsilon(c)}(\cdot)$ is the projection function that projects the current adversarial example back to the $\epsilon$-ball, $L$ is the loss function and $\theta$ is model parameters.

**Black-box Attack.** The black-box attacker only knows outputs of the model. One type of black-box attacks is query-based methods: generating adversarial examples by querying the target model multiple times to perform random sampling [1,19] or estimate gradients of the target model [20].
The other popular attack is transfer-based: based on a surrogate model, the attacker either generates adversarial data and then transfer them to the target model or base on them to estimate gradients of loss of the target model [5, 8].

### 3.3. Adversarial Training

Towards the resistance of adversarial examples, adversarial training (AT) [30] trains models on adversarial examples instead of clean data. Specifically, the adversarial examples are generated by PGD attack in Eq. 3 and AT can be formulated as a bi-level optimization task:

\[
\min_{\theta} \max_{c' \in B_c(c)} L(M(c'), y; \theta) \tag{4}
\]

### 4. Imperceptible Adversarial Attack by Iterative Visual and Structural Manipulation

This section introduces a strong adversarial attack by iteratively updating visual and structural information of inputs. Sec. 4.1 analyzes the vulnerability of deep GM. While Sec. 4.2 gives our adversarial attack with details in Sec. 4.3.

#### 4.1. Motivation

In Sec. 3.1, we introduce the common pipeline of deep two-graph matching as shown in Fig. 2: after building graphs by Delaunay triangulation [11], node features are obtained via a feature extractor \( f \) based on the keypoint locations and edge features are constituted based on node features and topology information of \( G^1, G^2 \), after which the affinity matrix \( K \) is initialized based on the node (edge) features. The initialized \( K \) is sent to the affinity learning layer \( g \) e.g. GNNs to learn the node-to-node and edge-to-edge similarity. Finally the predicted permutation matrix \( X \) gets obtained by the correspondence solver \( h \).

We include the straight forward idea of attacking the image pixels. Besides, we can infer from the above pipeline that the location of keypoints \( (z^1, z^2) \) affects how features of keypoints are extracted from the image and directly determines the graph structure derived by Delaunay triangulation. However, the location of keypoints suffers from its inherent instability due to the randomness of human labeling or keypoint detectors, which means small yet malicious noise could be easily added without being detected. Therefore, we also propose to perturb on keypoint locations.

#### 4.2. Objective Design

Given the analysis above, we explore a way of attacking both the image and graph through perturbing image pixel and keypoint locations simultaneously. We propose a joint optimization objective function as follows:

\[
\max_G \max_{c' \in C} L(c', z', G^1, G^2, X^{gt}; \theta) \tag{5}
\]

\[\text{s.t. } d_\infty(c', c) \leq \epsilon_c \quad d_\infty(z', z) \leq \epsilon_z\]

where \( X^{gt} \) is the ground-truth permutation; \( \epsilon_c \) and \( \epsilon_z \) are the perturbation budget to control how imperceptible the adversarial examples are to humans. Note that after perturbing the keypoint locality \( z' \), we further reconstruct the hidden graph \( G^2 \) based on Delaunay triangulation to boost the attack effectiveness. The pseudo code is given in Alg. 1.

#### 4.3. Implementation

Since existing deep GM allows end-to-end learning, we can readily implement a PGD-like attack on pixels and keypoint locations by maximizing loss in Eq. 3. We denote

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**Algorithm 1** Adversarial Attack with Visual and Structural Manipulation (VS-Attack).

**Input:** A pair of images \( c = (c^1, c^2) \), its keypoint sets \( z = (z^1, z^2) \), and its two graphs \( (G^1, G^2) \); loss function \( L \) and model parameters \( \theta \); perturbation budget \( (\epsilon_c, \epsilon_z) \), perturbation steps \( m \), and step size \( \alpha \); ground-truth matching \( X^{gt} \).

**Output:** Perturbed image \( c' \), keypoint \( z' \), and graph pair \((G^{1'}, G^{2'})\).

Initialize the adversarial example \( c_0, z_0 \leftarrow c, z \).

for \( k \) in \((0, 1, \ldots, m - 1) \) do

1. Calculate gradients: \( \{g(c'_k), g(z'_k)\} \leftarrow \{\nabla_{c'_k} L(c'_k, z'_k, X^{gt}; \theta), \nabla_{z'_k} L(c'_k, z'_k, X^{gt}; \theta)\} \)
2. Clip & Update pixel and keypoint: \( \{c'_k, z'_k\} \leftarrow \{\Pi_{B_\epsilon(c)}(c'_k + \alpha \text{sign}(g(c'_k))), \Pi_{B_\epsilon(z)}(z'_k + \alpha \text{sign}(g(z'_k)))\} \) via Eq. 3.
3. Update graph: \((G^{1'}_k, G^{2'}_k) \leftarrow z'_k \) by Delaunay triangulation.

end for
adversarial attacks on keypoint locations as the \textit{locality} attack, attacks on image pixels as the \textit{pixel} attack, and attacks on both of them as the \textit{combo} attack. To make our adversarial visual graph imperceptible, for pixel attack, we constrain the perturbation budget $\epsilon_z$ as $8/255$ while for locality attack, $\epsilon_z$ is set as $8$ (the image size is $256 \times 256$). An adversarial attack example is visualized on the left of Fig. 2. It confirms the imperceptibility of our adversarial attack.

5. Appearance Structure Adversarial Training for Deep Visual Graph Matching

In this section, we first analyze the attack pattern and show that appearance similar keypoints are more easily to be confused via statistics analysis. In Sec. 5.1, we propose a regularizer to encourage their difference. Sec. 5.2 and 5.3 show our defense mechanism using adversarial training.

5.1. Appearance Aware Regularizer

\textbf{Motivation.} As shown in Fig. 3b, keypoints of an object from the real-world images often contain similar appearance features, such as the four wheels of a car, on which humans depend to recognize the object. Such an appearance similarity can be summarized by three cases: shape similarity, texture similarity, and structure symmetry. Note that some similar keypoints could satisfy two or all cases, e.g., the left and right headlight of a car. We observe that under adversarial attacks, those appearance-similar keypoints are more likely to be mismatched: in Fig. 3b, the original $100\%$ matching accuracy between two cars drops to $0\%$ after being attacked and the attacker fools our GM solver by implicitly disturbing pairs of appearance-similar keypoints, e.g., the mismatched left and right side of the side-view mirror. Fig. 3c further validates our assumption: we attack all image pairs of “car” class and find that keypoints that are appearance-similar are intended to be mismatched with each other, which motivates us to utilize adversarial attack to discover the similarity relationship among keypoints.

\textbf{Objective Design.} In this paper, we propose a novel appearance aware regularizer (AAR) to explicitly enlarge the similarity among those appearance-similar keypoints in the probabilistic space of model outputs, i.e., based on the doubly-stochastic matrix $S \in [0,1]^{n \times n}$ in Eq. 2. We define $P=\{p_1,p_2,\ldots,p_n\}$ as the whole set of appearance-similar groups for each graph, in which each $p_i$ contains points which share similar appearance information.

After being attacked, we penalize those mismatched keypoints further away from the others in the same group $p_i$. We define an appearance aware matrix $R \in \mathbb{R}^{n \times n}$ which indicates the disparity among similar keypoints:

$$R_{i,j} = \begin{cases} 1.0 & \text{if } X_{i,j}^{gt} = 1 \text{ and } X_{i,j} \neq 1 \\ -1.0 & \text{if } X_{i,j}^{gt} = 0 \text{ and } i, \text{map}(j) \in p_k, p_k \in P \\ 0.0 & \text{otherwise} \end{cases} \quad (6)$$

where $\text{map}(\cdot) : j \in [n] \rightarrow i \in [n]$ projects the keypoint index in graph $G^2$ back to the matched index in graph $G^1$ based on $X^{gt}$ such that the margin between $i$ and $j$ would get penalized in the probabilistic space if $i$ and $\text{map}(j)$ are appearance-similar in $G^1$. Note that Eq. 6 focuses on those mismatched keypoints. For correctly matched keypoints of $G^1$ after being attacked, the corresponding row of $R$ is set as $0$, with no explicit penalty. Let $R = (r_1, r_2, \ldots, r_n)^\top$ and each $r_i$ means the matching probabilistic distribution of the keypoint $z_i^{1}$ of $G^1$ over all keypoints $z_i^{2}$ of $G^2$:

$$r_i = 0, \text{ if } X_i = X_i^{gt} \quad (7)$$

where $X_i$ and $X_i^{gt}$ denote the $i$th row data of the two matrices. Finally, our appearance aware regularizer (AAR) is:

$$\text{AAR} = -R \odot S = -\sum_{i=1}^{n} \sum_{j=1}^{n} R_{i,j} S_{i,j} \quad (8)$$

where $\odot$ means the element-wise matrix multiplication.

\textbf{Implementation.} First, based on our observation in Fig. 3, we utilize the adversarial attack to discover the appearance similarity among keypoints. Fig. 4 shows a working pipeline of our proposed AAR. After getting the attacked permutation matrix, we utilize the ground-truth matrix to map the matched keypoint index in $G^2$ back to that in $G^1$. For example, we have $a \rightarrow 1$, $b \rightarrow 2$, and $c \rightarrow 0$, then...
Finally, we propose a new defense algorithm to train our deep GM solver on those adversarial examples. On Eq. 5, we can generate adversarial visual graphs and find appearance-similar groups. The pseudo code is given in Alg. 2.

![Figure 4. Pipeline of our Appearance Aware Regularizer starting from a doubly-stochastic matrix. A discrete permutation matrix is obtained via Hungarian algorithm [26]. AAR first takes the attacked permutation matrix and the ground-truth to build the “reverse” permutation matrix which reveals the matching relationship in a single graph. We next perform a depth-first search to discover the appearance-similar groups of a graph. Then we build the appearance aware matrix based on the ground-truth matrix (recall our supervised setting). Finally, we utilize that matrix to mask the doubly-stochastic matrix to obtain the AAR matrix (see Alg. 2).](image)

Algorithm 2 Appearance Aware Regularizer (AAR).

**Input:** A pair of images $c = (c^1, c^2)$, its keypoint sets $z = (z^1, z^2)$, and its two graphs $(G^1, G^2)$; NGM solver $M$ and model parameters $\theta$; perturbation budget ($\epsilon_c$, $\epsilon_x$); doubly-stochastic matrix $S$, predicted permutation $X$, ground-truth permutation matrix $X^{gt}$.

**Output:** AAR matrix.

Obtain adversarial $c'$ and $z'$ via VS-Attack on $c$, $z$ by Alg. 1. Attacked permutation $X' \leftarrow M(c', z'; \theta)$.

* Working pipeline of building AAR shown in Fig. 4:
1. Build “reverse” permutation $X^{rev}$ in Eq. 9 by $X'$ and $X^{gt}$.
2. Find appearance-similar groups $P = (p_1, p_2, \ldots, p_m)$ by depth-first search on $X^{rev}$.
3. Build appearance aware matrix $R$ in Eq. 6 and Eq. 7;
4. Build AAR matrix by masking $S$ with $R$ in Eq. 8;

where the regularization term AAR follows the definition of Eq. 8, and $\beta$ is the tunable scaling parameter that balances the two parts of the final loss.

5.3. Implementation

We choose the state-of-the-art GM network NGMv2 as our defense baseline. In line with NGMv2, for Eq. 10a, we adopt the binary cross entropy (BCE) as the loss:

$$L(c, z, G, X^{gt}; \theta) = -\sum_{i=1}^{n} \sum_{j=1}^{n} X_{i,j}^{gt} \log S_{i,j} + (1 - X_{i,j}^{gt}) \log (1 - S_{i,j})$$

Since we craft our adversarial data as inputs via Eq. 10b, we also calculate AAR based on the attacked soft permutation matrix $S'$. Moreover, a burn-in period is introduced to obtain a better trade-off between clean accuracy and robustness. We generate weaker adversarial examples in the initial period of the training process because strong adversarial examples may hurt the generalization ability of models [53] when our solver is not properly learned. We choose $\beta$ as 1.5, burn-in period as 5 across all variants of ASAR-GM.

6. Experimental Evaluation

6.1. Evaluation Settings

**Dataset.** We evaluate keypoint matching on Pascal VOC dataset [14] with Berkeley annotations [4] and test the generalization ability of our method on Willow ObjectClass dataset [9]. We follow the protocol of [44] and filter out poorly annotated images and get 7,020 training samples and 1,682 testing samples. Experiments run on Intel(R) Xeon(R) E5-2678 v3 CPUs (2.50GHz) and 8 GTX 2080 Ti GPUs. The model is implemented by PyTorch.

**Graph Matching Baselines.** We validate the effectiveness of our adversarial attack over representative deep GM models: PCA-GM [45], BBGM [34], CIE-H [48], and NGMv2 [44]. For reproducibility, we apply the same training configuration of NGMv2 for defense and use the check-
Table 2. White-box robust accuracy (%) on Pascal VOC of (non-)robust models under various attacks. Adversarial examples are generated using the default loss designed for every model. “Overall” denotes mean accuracy across all data columns for each one. BBGM seems robust to current white-box attack pipeline, but it is probably due to its unique way of approximating gradients, and we show it is non-robust to black-box attack in Table 3. ASAR-GM (config 1) also boosts the accuracy of NGMv2 on clean examples.

Table 3. Black-box robust accuracy (%) on Pascal VOC of (non-)robust models under various attacks. All adversarial examples are generated based on pretrained NGMv2 baseline using binary cross entropy (BCE) loss. Same “Overall” as in Table 2.

points of other GM models collected by ThinkMatch\(^2\).

**Attack Models.** We evaluate robustness of models with three types of adversarial attacks, pixel, our locality and combo attack, based on the attack scale introduced in Sec. 4.3. For each type of attack, we perform (weak) FGSM and (strong) PGD-10 attack respectively. We select PGD-50 combo attack as the possible strongest attack to benchmark the empirical lower bound of robustness. The perturbation budget is set as \(\epsilon_{\text{pix}} = 8/255\) for pixel attack, \(\epsilon_{\text{loc}} = 8\) for locality attack, and the same \(\epsilon_{\text{pix}}\) and \(\epsilon_{\text{loc}}\) for combo attack.

**Defense Models.** Similar to our attack models, we use adversarial training (AT) with different types of adversarial examples as our defense baseline: pixel AT with pixel attack and locality AT with locality attack. All defense baselines are also trained against adversarial data with different attack strengths from (weak) FGSM to (strong) PGD-10 attack.

6.2. Experimental Results

**White-box attack results.** Table 2 shows robustness of deep GM baselines and variants of NGMv2 models under white-box attacks. On the attacker side, aligned with our analysis in Sec. 4.1, our PGD-50 combo attack becomes the strongest attack among all attack baselines and consistently degrades the matching performance across all baseline models by a notable margin. For example, accuracy of NGMv2 baseline drops from 80.4\% to 21.46\% under this attack. On the defender side, our ASAR-GM exhibits superior robustness against all adversarial attacks compared to defense baselines. Note that we implement three versions of ASAR-GM and the only difference among them is the attack strength of adversarial data as inputs to ASAR-GM after the burn-in period ends. Specifically, (weaker) single-step pixel attack is applied for config 1, and (stronger) single-step combo attack is used for config 2 while (much stronger) two-step combo attack is used for config 3. ASAR-GM with config 1 achieves a better clean accuracy, 81.15\% even than baseline, 80.4\% while config 2 achieves better robustness with a little degradation of accuracy and config 3 further boosts robustness at a higher cost of accuracy, which agrees with the commonsense that the effectiveness of defense depends on the strength of the attack used for training [30, 36]. These results show that ASAR-GM can bring a better generalization ability on both accuracy and robustness while standard AT often suffers from the trade-off between accuracy and robustness [41, 52].

**Black-box attack results.** We choose NGMv2 baseline model as the surrogate model and transfer adversarial examples crafted on NGMv2 to every target model. Experimental results on Table 3 demonstrate remarkable robustness of ASAR-GM against transfer-based attacks. Note that different from other baselines, robustness of BBGM drops by a notable margin when being attacked under black-box attack compared to white-box attack: accuracy under PGD-10 combo attack drops from 64.66\% to 44.27\%. The reason might be the gradient estimation of BBGM is a linear approximation of a piece-wise linear solver, which can be inaccurate and mislead the attacker in white-box setting.

\(^2\) https://github.com/Thinklab-SJTU/ThinkMatch
Therefore, we ascribe the false sense of security of BBGM to obfuscated gradients [2].

**Generalization study.** Table 5 shows that ASAR-GM generalizes better from “seen” Pascal VOC to “unseen” Willow ObjectClass than standard training: improving the clean accuracy from 83.22% to 90.37%, which further corroborates that ASAR-GM learns better features of keypoints.

**Ablation study.** Table 4 validates the necessity of every defense component of ASAR-GM. For **locality** attack, since it directly affects graph construction, we further devise three types: “location”, “structure”, “both”. For “location”, we choose to only perturb keypoint locations while preserving the original graph structure. For “structure”, we reconstruct the graph structure based on the perturbed keypoint locations while the keypoint location itself remains unchanged during inference. For “both”, both keypoint locations and the following graph construction get perturbed and then join the matching pipeline together. We first implement a random version of the “both” locality attack and experimental results shows no benefit of such randomness on clean accuracy with little improvement of robustness. Secondly, we compare standard AT<sub>F<sub>FGSM with(out) our regularization term, namely AAR and AAR achieves both better accuracy and robustness. Finally, for locality attack, compared with performance of baseline model under random attack, our perturbations on graph structure greatly improve model generalization ability, and those on both location and structure further enhance such advantage thus we choose “both” locality attack in our final model.

**More attack baselines.** To fully evaluate robustness, we conduct stronger white-box attacks with more iterations or using the target label, and another black-box attack, MI-FGSM [12]. See Appendix A for details.

**Applicability of locality attack and AAR.** We apply our locality attack and AAR to another baseline, PCA-GM and verify the applicability. See Appendix B for details.

**Consideration of adaptive attack.** By the adaptive attack criterion [39], we generate adversarial attacks via maximizing the original loss with our AAR loss together. ASAR-GM achieves 69.1% compared to PGD-50 combo attack 69.6%, signifying the robustness of our method.

7. **Conclusion**

In this paper, we have taken the initiative to study the vulnerability of deep (visual) GM models and design an effective adversarial attack, aiming at perturbing keypoint localities and its hidden graphs together. We further propose our defense strategy whereby an appearance-aware regularizer is developed to explicitly enlarge the disparity among the similar keypoints. Experiments on real dataset demonstrate the effectiveness of our attack and defense algorithm. Moreover, our locality attack can serve as a data augmentation and improve model generalization ability on clean test data, bringing a new SOTA on matching accuracy.
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